How to Solve Drug Dosage Problems

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General Information

There are three different types of measurements you will encounter when dealing with medications: Household, Apothecary, and Metric.

<table>
<thead>
<tr>
<th>Type</th>
<th>Number</th>
<th>Solids</th>
<th>Liquids</th>
</tr>
</thead>
<tbody>
<tr>
<td>Household</td>
<td>Whole numbers and fractions <strong>before</strong> unit. Ex: 1 ½ T</td>
<td>Teaspoons (tsp, t)</td>
<td>Drop (gtt)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Tablespoons (Tbs, T)</td>
<td>Ounce (oz)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Pounds (lb)</td>
<td>Cup (c)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Pint (pt)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Quart (qt)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Glass</td>
</tr>
<tr>
<td>Apothecary</td>
<td>Whole numbers, fractions, and Roman Numerals <strong>after</strong> unit. Ex: gr 15 ½ or dr iss</td>
<td>Grains (gr)</td>
<td>Minum (m)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Drams (dr or Ʒ)</td>
<td>Fluid Dram (dr or Ʒ)</td>
</tr>
<tr>
<td>Metric</td>
<td>Whole numbers and decimals <strong>before</strong> unit (always put a 0 in front of the decimal. Ex: 0.15 mL</td>
<td>Grams (g)</td>
<td>Liters (L)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Meter (m)</td>
<td></td>
</tr>
</tbody>
</table>

Note: When two system-to-system conversion factors exist, consider the unit of the final answer. For example, if it is necessary in the drug dosage problem to convert a dosage from grains to mg, use the gr \( 1 = 60 \text{ mg} \) conversion factor.

**Approximate Conversion Factors**

**Solid conversions**

- gr 1 = 60 mg
- gr 15 = 1 g
- 2.54 cm = 1 in
- 2.2 lb = 1 kg

**Fluid conversions**

- 1 oz = dr 8 or Ʒ 8
- m 15 = 1 mL = 1 cc
- 4 mL = fluid dr 1 = Ʒ 1
- 15 mL = 3 t = 1 T
- 30 mL = 1 oz

**Extended conversions**

- 1 kg = 1000 g = 2.2 lbs
- 1 L = 1000 mL = 33 1/3 oz = 200 t = 66 2/3 T = Ʒ 250
Visual Conversions

“The Grain Clock”
Convert grains to mg

<table>
<thead>
<tr>
<th>Grains (gr)</th>
<th>Milligrams (mg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>60</td>
</tr>
<tr>
<td>½</td>
<td>30</td>
</tr>
<tr>
<td>¾</td>
<td>45</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Time (hour)</th>
<th>Minutes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>60</td>
</tr>
<tr>
<td>½</td>
<td>30</td>
</tr>
<tr>
<td>¾</td>
<td>45</td>
</tr>
</tbody>
</table>

Inches to centimeters

1 inch = 2.54 cm

Roman Numerals

<table>
<thead>
<tr>
<th>Roman</th>
<th>Numerals</th>
</tr>
</thead>
<tbody>
<tr>
<td>½</td>
<td>ss or ss</td>
</tr>
<tr>
<td>1</td>
<td>I or i or I</td>
</tr>
<tr>
<td>2</td>
<td>II or ii or II</td>
</tr>
<tr>
<td>3</td>
<td>III or iii or III</td>
</tr>
<tr>
<td>4</td>
<td>IV or iv (i before v = 5-1) or IV</td>
</tr>
<tr>
<td>5</td>
<td>v or v</td>
</tr>
<tr>
<td>10</td>
<td>x or x</td>
</tr>
<tr>
<td>15</td>
<td>xv or xv</td>
</tr>
<tr>
<td>19</td>
<td>xix [10 + (10-1)] or xix</td>
</tr>
<tr>
<td>20</td>
<td>xx or xx</td>
</tr>
</tbody>
</table>
Converting Between Units

Use of One Conversion Factor:

To convert from one unit to another, begin with the unit assigned. Next find a conversion factor that relates the unit assigned to the unit needed. Then multiply the unit assigned by the found conversion factor. This calculation results in the new unit.

Example: Convert 120 mg to gr_______.

Step one: Think of a conversion factor that relates mg and gr. 60 mg = gr 1 (This can be used as either 60 mg/gr 1 or gr 1/60 mg)

Step two: set up the multiplication equation.

\[ \frac{120 \text{ mg} \cdot \frac{\text{gr}}{60 \text{ mg}}}{60 \text{ mg}} = \text{gr} \]

Note: when using the conversion factor, always place the needed unit on top.

Step three: Solve the equation.

First cancel mg units, \[ \frac{120 \text{ mg} \cdot \frac{\text{gr}}{60 \text{ mg}}}{60 \text{ mg}} = \text{gr} \]

Then solve the equation \[ 120 \cdot \frac{\text{gr}}{60} = \text{gr} \]

Therefore: 120 mg = gr 2

Use of Multiple Conversion Factors:

If a conversion factor for the two units does not exist, then proceed through another unit to obtain the unit needed.

Example: Convert 1 T to ____oz.

Step one: Try to find a conversion factor that relates tablespoons to ounces. Looking at the list, there is not a conversion factor relating tablespoons and ounces. Therefore, two conversion factors are needed: 1 T = 15 mL and 30 mL = 1 oz.

Step two: Set up the equations

\[ \frac{1 \text{ T} \cdot 15 \text{ mL}}{1 \text{ T}} = \text{mL} \]

\[ \frac{\text{mL} \cdot 1 \text{ oz}}{30 \text{ mL}} = \text{oz} \]

Step three: Solve the equations.

\[ 1 \text{ T} \cdot 15 \text{ mL} \div 1 \text{ T} = 15 \text{ mL} \]

\[ 15 \text{ mL} \cdot 1 \text{ oz} \div 30 \text{ mL} = 0.5 \text{ oz} \]

Therefore: 1 T = 0.5 oz
Converting Between Metric Units

To convert between metric units, simply move the decimal place. The easiest way to remember which way to move the decimal as well as the number of places to slide it is the mnemonic: “King Henry died by drinking chocolate milk . . merrily.”

<table>
<thead>
<tr>
<th>symbol</th>
<th>King</th>
<th>Henry</th>
<th>died</th>
<th>by</th>
<th>drinking</th>
<th>chocolate</th>
<th>milk</th>
<th>merrily</th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>kilo</td>
<td>hector</td>
<td>Deca</td>
<td>“base”</td>
<td>deci</td>
<td>centi</td>
<td>milli</td>
<td>micro</td>
</tr>
<tr>
<td>Ex.</td>
<td>kg</td>
<td>hg</td>
<td>Dg</td>
<td>gram</td>
<td>dg</td>
<td>cg</td>
<td>mg</td>
<td>mcg</td>
</tr>
</tbody>
</table>

† there are three decimal places between m and mc. This is commonly forgotten!

**Using the “King Henry” method** to convert between metric units involves locating the starting place then sliding the decimal to the desired unit and adding zeros as needed.

**Example 1:** Convert 25.3 g to ________mg

Step one: The given unit is gram, so start at “b”.

Step two: The ending place is m, so slide the decimal from “b” to “m”.

Step three: **King Henry died by drinking chocolate milk . . merrily**

\[
\begin{align*}
25.3 & \rightarrow 25.300 \rightarrow 25,300 \text{ mg} \\
\text{Therefore: } 25.3 \text{ g} &= 25,300 \text{ mg}
\end{align*}
\]

**Example 2:** Convert 300 mcg to ________mg

Step one: The given unit is mcg, so start at “mc”.

Step two: The ending place is m, so slide the decimal from “mc” to “m”.

Step three: **King Henry died by drinking chocolate milk . . merrily**

\[
\begin{align*}
300 & \rightarrow 0.300 \rightarrow 0.300 \text{ mg} \\
\text{Therefore: } 300 \text{ mcg} &= 0.300 \text{ mg}
\end{align*}
\]
Calculating Drug Dosages

When performing drug calculations, one of the following four methods should be used: **Ratio (Rainbow) Method**, **Proportion Method**, **Formula Method**, or **Dimensional Analysis**. Each of these methods works as well as the others. However, once the student decides which method is the most comfortable for them, they should stick with that method and not switch back and forth between the different methods.

**Ratio (Rainbow):**
- Step one: Set up ratios.
- Step two: Multiply means and extremes
- Step three: Solve for “x” algebraically.

**Proportion:**
- Step one: Set up proportions
- Step two: Cross multiply
- Step three: Solve for “x” algebraically

**Formula:**
\[ D \times Q = \text{answer} \]
\[ \frac{D \text{ (dose ordered)}}{H \text{ (on hand)}} \times \frac{Q \text{ (unit quantity)}}{H \text{ (on hand)}} = \text{answer} \]

**Dimensional Analysis:**
\[ D \times Q = \text{answer} \]
\[ \frac{D \text{ (dose ordered)}}{H \text{ (on hand)}} \times \frac{Q \text{ (unit quantity)}}{H \text{ (on hand)}} = \text{answer} \]

Use drug calculations when calculating the quantity of medications needed for a patient and the strength of medication is already known.

**Example:** If the doctor orders 20 mg of Benadryl, and 10 mg tablets are available, how many tablets should be given to the patient?

**Ratio (Rainbow) Method**
We know that 10 mg = 1 tablet, and we need 20 mg in an unknown number of tablets.

- **Step one:** Set up ratios.
  \[ 10 \text{ mg} : 1 \text{ tab} = 20 \text{ mg} : x \text{ tab} \]

Notice that on both sides of the equation, mg comes first, then tablets. This is **very important**. It does not matter which unit comes first, as long as units are in the same order on both sides of the equal “=” sign.

- **Step two:** Multiply means and extremes
  \[ 10 \text{ mg} \times x \text{ tab} = 1 \text{ tab} \times 20 \text{ mg} \]

- **Step three:** Solve for “x” algebraically.
  \[ x \text{ tab} = \frac{1 \text{ tab} \times 20 \text{ mg}}{10 \text{ mg}} \]
  \[ x = 2 \text{ tablets} \]
Proportion Method

Step one: Set up proportions
\[ \frac{10 \text{ mg}}{1 \text{ tab}} = \frac{20 \text{ mg}}{x \text{ tab}} \]

Step two: Cross multiply
\[ 10 \text{ mg} \cdot x \text{ tab} = 20 \text{ mg} \cdot 1 \text{ tab} \]

Step three: Solve for “x” algebraically
\[ x \text{ tab} = \frac{20 \text{ mg} \cdot 1 \text{ tab}}{10 \text{ mg}} \]
\[ x = 2 \text{ tablets} \]

Formula Method

\[ \frac{D}{H} \cdot \frac{Q}{10 \text{ mg}} = \frac{20 \text{ mg} \cdot 1 \text{ tab}}{10 \text{ mg}} \]

Therefore: give the patient 2 tablets.

Dimensional Analysis

\[ \frac{D}{H} \cdot \frac{Q}{10 \text{ mg}} = \frac{20 \text{ mg} \cdot 1 \text{ tab}}{10 \text{ mg}} \]

Useful Formulas for Calculating Drug Calculation Problems

Calculating BSA (m²):

\[ \sqrt{\frac{\text{Lb} \times \text{in}}{3131}} \quad \text{or} \quad \sqrt{\frac{\text{kg} \times \text{cm}}{3600}} \]

• Round to hundredths place after taking the square root

Example: If a patient weighs 140 lb and is 62 inches tall, calculate the BSA by simply plugging the numbers into the formula and solving.

\[ \sqrt{\frac{140 \text{ lb} \times 62 \text{ in}}{3131}} \]

\[ 140 \times 62 = 8,680 \]
\[ 8,680 \div 3131 = 2.77 \]
\[ \sqrt{2.77} = 1.66 \text{ m}^2 \]

• Round to hundredths place
• Answer is always in m²
Calculating a child’s dosage using an adult dosage:

\[
\text{Child’s BSA} \times \text{adult dosage} = \text{child’s dosage} \\
1.7 \text{ m}^2
\]

**Example:** The normal adult dosage of a medication is 150 mg. The child weighs 32 kg and is 120 cm tall. How much medication should be given to the child?

**Step one:** Find the child’s BSA. To do so, use the formula given above.

\[
\sqrt{32 \text{ kg} \times 120 \text{ cm}} = \sqrt{1.0666...} = 1.032792... \text{ m}^2 = 1.03 \text{ m}^2
\]

**Step two:** Use the child’s dosage formula.

\[
\frac{1.03 \text{ m}^2}{1.7 \text{ m}^2} \times 150 \text{ mg} = 90.88 \text{ mg}
\]

Calculating Flow Rate in mL/h:

\[
\text{Total mL ordered} = \text{mL/h} \quad \text{(must round to a whole number)} \\
\text{Total hours ordered}
\]

**Example:** Calculate the flow rate for an IV of 1,820 mL Normal Saline IV to infuse in 15 h by controller. Flow rate = ________ mL/h

\[
1,820 \text{ mL} = 121.33 \text{ mL/h} = 121 \text{ mL/h}
\]

**Calculating Flow Rate in gtt/min:**

\[
\frac{\text{Volume (mL)}}{\text{Time (min)}} \times \text{drop factor (gtt/mL)} = \text{Rate (gtt/min)} \quad \text{(MUST be whole #)}
\]

**Example:** The physician orders Lactated Ringer’s IV at 150 mL/h. The drop factor is 15 gtt/mL. Find the flow rate in gtt/min.

\[
150 \text{ mL} \times 15 \text{ gtt} = 37.5 = 38 \text{ gtt/min}
\]
Calculating Heparin Dosages:

Order: D5W Heparin 40,000 U in 1,000 mL D5W to infuse at 40 mL/h. What is the hourly heparin dosage?

Find how many Units are in 40 mL.

\[
\frac{40,000 \text{ U}}{1,000 \text{ mL}} \times \frac{x \text{ U}}{40 \text{ mL}} = \text{Cross multiply}
\]

\[
x \text{ U} \times 1,000 \text{ mL} = 40,000 \text{ U} \times 40 \text{ mL}
\]

\[
\text{then divide by } 1,000 \text{ mL}
\]

\[
\frac{40,000 \text{ U} \times 40 \text{ mL}}{1,000 \text{ mL}} = \frac{1,600,000 \text{ U}}{1000} = 1600 \text{ U/hr}
\]

Converting from °F to °C or °C to °F:

\[
\text{°F} = 1.8 \times (\text{°C}) + 32
\]

• Carry to hundredths and round to tenths

\[
\text{°C} = \frac{\text{°F} - 32}{1.8}
\]

Example: What is 212 °F in Celsius?

\[
\text{°C} = \frac{212 - 32}{1.8} \quad \text{°C} = \frac{180}{1.8} \quad \text{°C} = 100°
\]

Example: What is 37 °C in Fahrenheit?

\[
\text{°F} = 1.8 \times (\text{°C}) + 32 \quad \text{°F} = 1.8 (37) + 32 \quad \text{°F} = 66.6 + 32 \quad \text{°F} = 98.6°
\]

Helpful Websites

There are many helpful drug dosage calculation websites. The following links include practice problems and solutions. We encourage you to use them to your advantage. After all, the best way to become proficient at solving drug dosage problems is to PRACTICE!

http://nursesaregreat.com/articles/drugcal.htm

http://www.testandcalc.com/drugcalc_legacy/index.asp

http://www.unc.edu/~bangel/quiz/quiz5.htm

http://nursing.flinders.edu.au/students/studyaids/drugcalculations/page.php?id=1